

## 30 Chapter 2 Force Systems

## SAMPLE PROBLEM 2/2

Combine the two forces  $\mathbf{P}$  and  $\mathbf{T}$ , which act on the fixed structure at  $B$ , into a single equivalent force  $\mathbf{R}$ .

- Graphical solution.** The parallelogram for the vector addition of forces  $\mathbf{T}$  and  $\mathbf{P}$  is constructed as shown in Fig. *a*. The scale used here is 1 in. = 800 lb; a scale of 1 in. = 200 lb would be more suitable for regular-size paper and would give greater accuracy. Note that the angle  $\alpha$  must be determined prior to construction of the parallelogram. From the given figure

$$\tan \alpha = \frac{\overline{BD}}{\overline{AD}} = \frac{6 \sin 60^\circ}{3 + 6 \cos 60^\circ} = 0.866 \quad \alpha = 40.9^\circ$$

Measurement of the length  $R$  and direction  $\theta$  of the resultant force  $\mathbf{R}$  yields the approximate results

$$R = 525 \text{ lb} \quad \theta = 49^\circ \quad \text{Ans.}$$

- Geometric solution.** The triangle for the vector addition of  $\mathbf{T}$  and  $\mathbf{P}$  is shown in Fig. *b*. The angle  $\alpha$  is calculated as above. The law of cosines gives

$$R^2 = (600)^2 + (800)^2 - 2(600)(800) \cos 40.9^\circ = 274,300$$

$$R = 524 \text{ lb} \quad \text{Ans.}$$

From the law of sines, we may determine the angle  $\theta$  which orients  $\mathbf{R}$ . Thus,

$$\frac{600}{\sin \theta} = \frac{524}{\sin 40.9^\circ} \quad \sin \theta = 0.750 \quad \theta = 48.6^\circ \quad \text{Ans.}$$

**Algebraic solution.** By using the  $x$ - $y$  coordinate system on the given figure, we may write

$$R_x = \Sigma F_x = 800 - 600 \cos 40.9^\circ = 346 \text{ lb}$$

$$R_y = \Sigma F_y = -600 \sin 40.9^\circ = -393 \text{ lb}$$

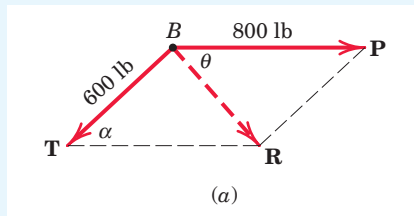
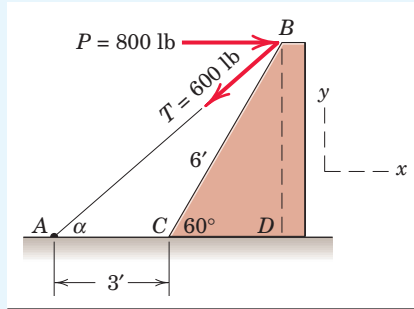
The magnitude and direction of the resultant force  $\mathbf{R}$  as shown in Fig. *c* are then

$$R = \sqrt{R_x^2 + R_y^2} = \sqrt{(346)^2 + (-393)^2} = 524 \text{ lb} \quad \text{Ans.}$$

$$\theta = \tan^{-1} \frac{|R_y|}{|R_x|} = \tan^{-1} \frac{393}{346} = 48.6^\circ \quad \text{Ans.}$$

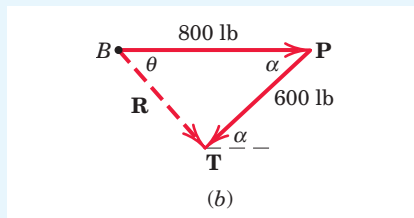
The resultant  $\mathbf{R}$  may also be written in vector notation as

$$\mathbf{R} = R_x \mathbf{i} + R_y \mathbf{j} = 346 \mathbf{i} - 393 \mathbf{j} \text{ lb} \quad \text{Ans.}$$



## Helpful Hints

- 1 Note the repositioning of  $\mathbf{P}$  to permit parallelogram addition at  $B$ .



- 2 Note the repositioning of  $\mathbf{F}$  so as to preserve the correct line of action of the resultant  $\mathbf{R}$ .

