

GLASGOW CALEDONIAN UNIVERSITY

QUESTIONS FOR DROP-IN

University for the Common Good

Jupiter

Question - Integration

First differentiate each of the following functions:

$$x^2 + 3x + 2$$

$$\Rightarrow x^2 + 3x$$

$$\diamond \frac{1}{3}x^3 + \frac{3}{2}x^2$$

Using your answers above, can you give the integral of f(x) = 2x + 3? i.e.

$$\int 2x + 3 \, \mathrm{d}x = ?$$

Question - Integration areas under curves

Write the integral notation for what integral you would need to calculate to find the area under the curve $f(x) = x^2 + 1$ between x = 1 and x = 4.

(You can do the calculation afterwards, if you wish)

Question - Definite integration

Given that the indefinite integral of cos(2x) + 4x is $\frac{1}{2}sin(2x) + 2x^2 + C$, calculate

$$\int_0^{\pi} \cos(2x) + 4x \, \mathrm{d}x$$

Question - Checking your answer

Use www.desmos.com/calculator or some other graphical calculator to sketch the function from the previous question $(\cos(2x) + 4x)$. Was the answer to the previous question positive or negative? Can you see why from the graph?

Question - Integration

Find the indefinite integral of the following function:

$$f(x) = \frac{1}{x^2} + \frac{1}{x} + 1 + x$$

Question - Integration

Given that the derivative of $\sin(4x + 3)$ is $4\cos(4x + 3)$ and that the derivative of $\cos(4x + 3)$ is $-4\sin(4x + 3)$ use one of these facts to find the following integral.

$$\int 24\cos(4x+3) \, \mathrm{d}x$$